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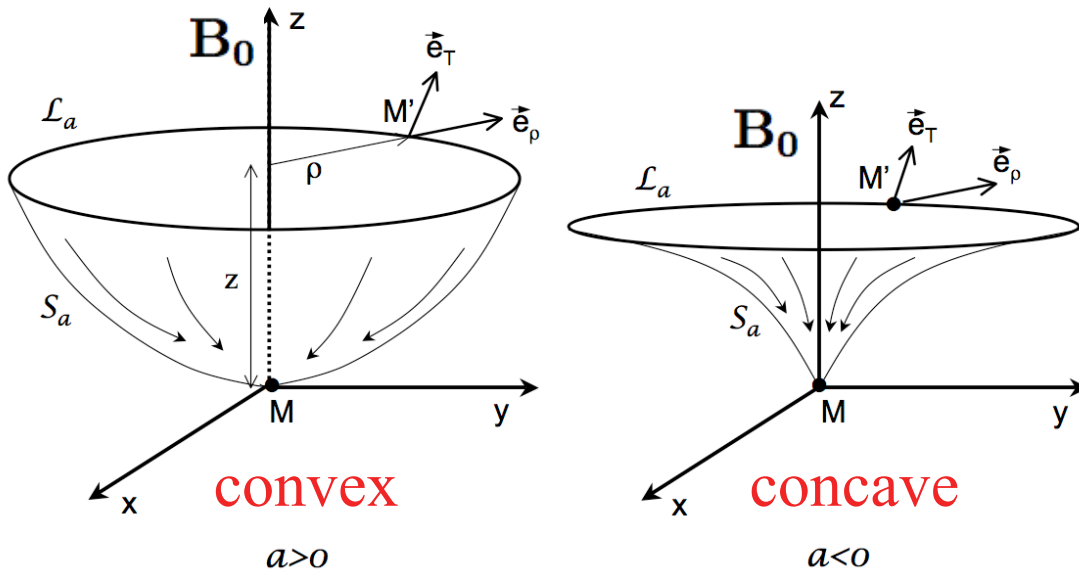
**« On the nature of anisotropy in  
solar wind turbulence »**

∃ a scaling relation between  $\perp$  and  $//$  correlation length scales

Is there a Kolmogorov MHD law in **space correlation** ?

# Anisotropic MHD

Let's consider a class of (local) axisymmetric MHD turbulence



$$\mathbf{F}^{\pm}(\mathbf{r}) = F_T^{\pm} \mathbf{e}_T$$

$$\mathbf{F}^{\pm}(\mathbf{r}) = \langle \delta \mathbf{z}^{\mp} (\delta \mathbf{z}^{\pm})^2 \rangle$$

$$z = f_a(\rho) = A \rho^{1+a}$$

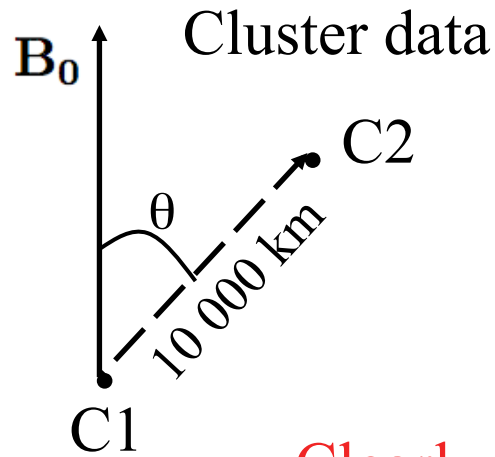
$a$  : degree of anisotropy

$\left\{ \begin{array}{l} a=0 : 3\text{D isotropic case} \\ a=-1 : 2\text{D isotropic case} \end{array} \right.$

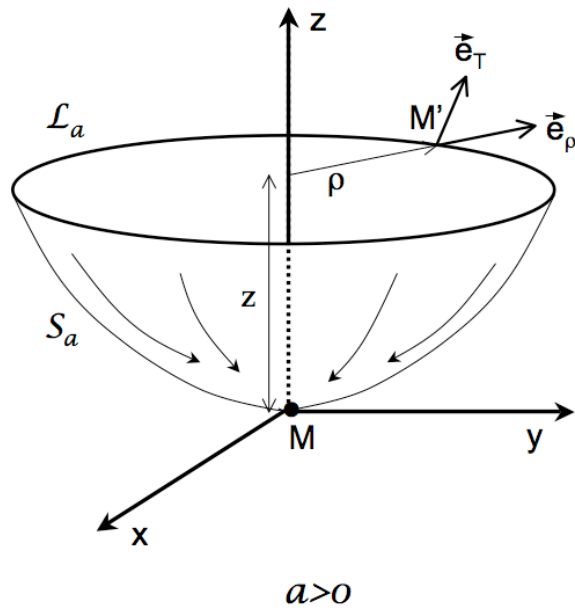
$$-4\varepsilon^{\pm} = \nabla \cdot \mathbf{F}^{\pm}(\mathbf{r}) = \frac{1}{\rho} \frac{\partial(\rho F_{\rho}^{\pm})}{\partial \rho} + \frac{\partial F_z^{\pm}}{\partial z}$$

$$\mathbf{F}^{\pm}(r, z) = -\frac{4}{3+a} \varepsilon^{\pm} \left( \rho \mathbf{e}_{\rho} + (1+a)z \mathbf{e}_z \right)$$

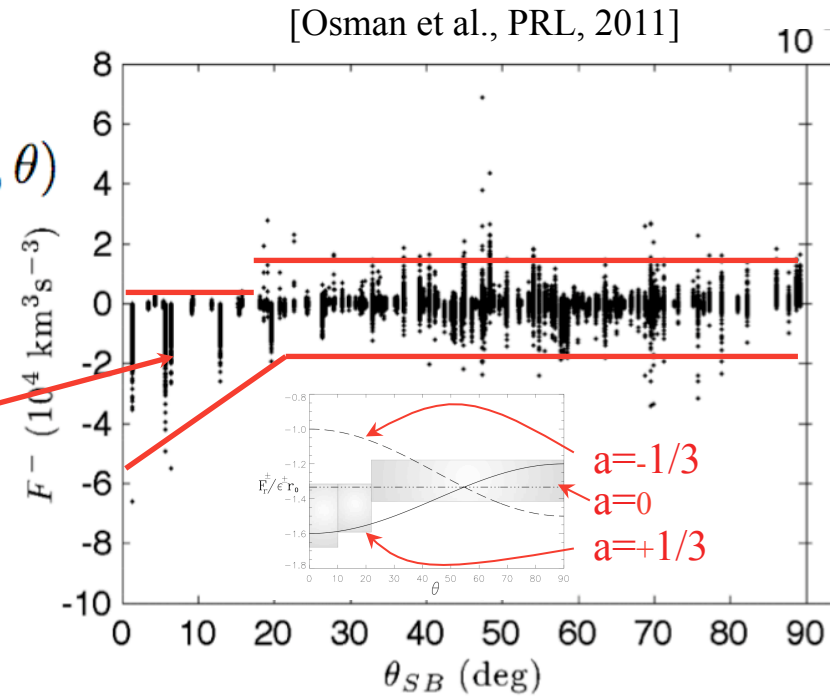
Exact vectorial law for a class of axisymmetric turbulence



Clearly more negative



$$F_r^-(r_0, \theta)$$



Theory says: 
$$F_r^\pm(r, \theta) = -\frac{4}{3+a} \epsilon^\pm r (1 + a \cos^2 \theta)$$

Compatible with a **convex** turbulence

→ *Galtier, ApJ, 2012*